

Dyes and Pigments 44 (2000) 123-129



# Precise PPP molecular orbital calculations of excitation energies of polycyclic aromatic hydrocarbons. Part 5<sup>th</sup> Spectroactive portion of fluoranthene derivatives

Kimihiro Hiruta <sup>a</sup>, Sumio Tokita <sup>a,\*</sup>, Tatsuya Tachikawa <sup>a</sup>, Kichisuke Nishimoto <sup>b</sup>

<sup>a</sup>Department of Applied Chemistry, Faculty of Engineering, Saitama University, 255 Shimo-Ohkubo, Urawa, Saitama, 338-8570 Japan <sup>b</sup>Institute for Fundamental Chemistry, 34-4 Takano-Nishihiraki-cho, Sakyo-ku, Kyoto, 606-8103 Japan

Received 26 June 1999; accepted 24 August 1999

### Abstract

For Pariser–Parr–Pople molecular orbital (PPP MO) calculations of the p-band of fluoranthene derivatives, the values of the spectrochemical softness (SCS) parameter k in a novel two centre electron repulsion integral new- $\gamma$  were evaluated based on the spectroactive portion (SP) of a molecular framework. The SP was determined by the character of MO calculated by the HMO method with reference to the structural analysis by ab initio MO calculations with 6-31G\* level. The calculated excitation energies of the p-band of fluoranthene derivatives using the new- $\gamma$  including k values based on the SP reproduced accurately the observed ones. © 1999 Elsevier Science Ltd. All rights reserved.

Keywords: PPP MO calculations; Fluoranthene derivatives; p-Band; New-γ; Spectrochemical softness parameter; Spectroactive portion

# 1. Introduction

In our previous papers dealing with PPP MO calculations of excitation energies of the p-band (nomenclature by Clar [2]: corresponds to Platt's  $^1L_{\rm a}$  band [3]) of alternate polycyclic aromatic hydrocarbons (PAHs) [4–6], the new- $\gamma$  [7] was successfully applied. The calculated excitation energies were greatly improved for many alternate PAHs in comparison with the calculated ones using the conventional N·M- $\gamma$  [8].

The SCS parameter k in the new- $\gamma$  can be evaluated based on the absolute hardness  $\eta$  of a given molecule [4], spectroactive portion (SP) of the molecular framework [5,6], or Dewar-type resonance energies [1]. The SP contributes mainly to the electronic spectra of PAHs [5], and it is the most favorable index to evaluate the SCS parameter k in the above three indices [1].

In this paper, we extend the evaluating method of the SCS parameter k in the new- $\gamma$  based on SP to non-alternate PAHs for precise calculation of the excitation energies of the longest absorption band (p-band). Formulae of non-alternate fluoranthene derivatives used for the calculation are shown in Fig. 1.

<sup>☆</sup> Part 4: Hiruta K, Tokita S, Nishimoto K. Dyes and Pigments, 1998;36:116. [part 4]

<sup>\*</sup> Corresponding author. Fax: +81-48-857-9653. E-mail address: tokita@apc.saitama-u.ac (S. Tokita).

### 2. MO calculations

PPP MO calculations were performed with a computer software revised PPP-PC [9], in which variable β approximation [10] and the conventional parameters set [9,11,12] were used as in our previous papers [1,4–6]. For two centre electron repulsion integral, the following new- $\gamma$  was used. To compare with the calculated results, the conventional N·M- $\gamma$  was also used. Twenty-five lower singly excited configurations were used in the CI calculations.

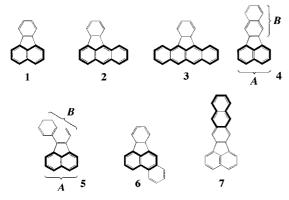


Fig. 1. Structural formulae of calculated non-alternate fluor-anthene derivatives; SP is represented using bold lines.

Table 1 Values of SCS parameter *k* corresponding to SP

Į <sup>a</sup>	2	3	4
$\overline{k}$	1.14	1.47	1.80

<sup>&</sup>lt;sup>a</sup> Number of six-membered rings contained in SP.

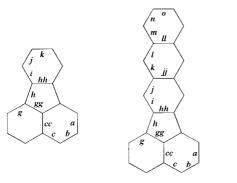


Fig. 2. Symboling scheme of compounds 1 and 7.

When the mobile  $\pi$ -electron polarization at the region between the r-th and the s-th atoms in a molecule is considered as follows,

$$R^+ - S^-$$
 and  $R^- - S^+$ 

the new- $\gamma$  is represented as in Eq. (1):

$$\gamma_{rs} = e^2 / [(R_{rs} + 2k_{rs}e^2)/(I_r - A_s + I_s - A_r)]$$
 (1)

where  $R_{rs}$  is the interatomic distance (in Å) between the r-th and the s-th atoms,  $e^2$  is 14.397  $eV\cdot Å$ ,  $I_r$  [ $I_s$ ] and  $A_r$  [ $A_s$ ] are the valence state ionization potential and the valence state electron affinity, respectively [7]. Essentially,  $k_{rs}$  is the relative magnitude of the dynamical polarizability of mobile  $\pi$ -electrons at the region between the r-th

Table 2 The observed and calculated carbon–carbon bond lengths (in  $\mathring{A}$ ) in compounds 1 and 7

Compound	Bond	Observed	Calculated ab intitio (6-31G*)	Calculated PPP (new-γ)
1	a	1.411	1.424	1.412
	b	1.368	1.366	1.383
	c	1.422	1.423	1.422
	cc	1.400	1.383	1.416
	g	1.367	1.360	1.390
	gg	1.411	1.413	1.426
	h	1.476	1.481	1.457
	hh	1.417	1.410	1.410
	i	1.384	1.380	1.404
	j	1.386	1.391	1.395
	k	1.379	1.387	1.400
7	a		1.422	1.410
	b		1.366	1.384
	c		1.422	1.421
	cc		1.387	1.416
	g		1.361	1.392
	gg		1.413	1.426
	h		1.479	1.452
	hh		1.458	1.433
	i		1.344	1.385
	j		1.440	1.427
	jj		1.430	1.428
	k		1.386	1.406
	l		1.393	1.407
	ll		1.422	1.426
	m		1.434	1.428
	n		1.349	1.377
	0		1.430	1.420

and the s-th atoms, namely, the 'spectrochemical softness' of  $\pi$ -electrons. When the value of  $k_{rs}$  is 1, the new- $\gamma$  is equivalent to the N·M- $\gamma$ . Large  $k_{rs}$  values are suitable for spectrochemically softer compounds such as polyacenes, except for benzene [4]. The k values shown in Table 1 were used for the calculation, corresponding to the number of six-membered rings in the SP [5].

The carbon–carbon bond lengths  $R_{c-c}$  calculated by PPP MO calculations can be evaluated from the Eq. (2) [10]

$$R_{c-c} = 1.517 - 0.180\rho \tag{2}$$

where  $\rho$  is the bond order.

Ab initio MO calculations with 6-31G\* basis set were performed with a GAUSSIAN 94 program [13].

The observed excitation energies of given PAHs in an inert solvent were extrapolated to those in the gas phase in order to minimize solvent effects [2].

### 3. Results and discussion

### 3.1. Fluoranthene (1)

Fluoranthene 1 can be built up from a benzene unit (Fig. 2), a naphthalene unit and two bonds  $\bf h$  and  $\bf n$  which combine both units. The  $\bf h$  and  $\bf n$  bonds essentially belong to a  $\pi$ -conjugated system. However, they possess the nature of a single bond. The observed bond lengths obtained from X-ray crystallographic analysis [14] and the ab initio MO

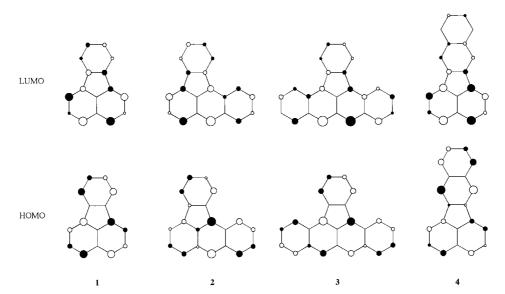


Fig. 3. The LCAO coefficients of HOMO and LUMO of compounds 1, 2, 3 and 4.

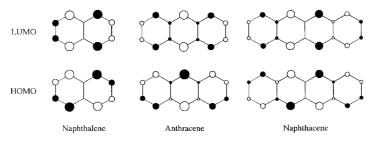


Fig. 4. The LCAO coefficients of HOMO and LUMO of polyacenes.

Table 3
The observed and calculated excitation energies (in eV) of the *p*-band of compounds 1–7

Compound	$E_{obs.}$ (gas phase)	$E_{\text{calc.}} [N \cdot M - \gamma](f)$	$E_{calc.}$ [new- $\gamma$ ](f)	Transition [N·M- $\gamma$ ] (coefficient)
1	3.57	3.61 (0.456)	3.56 (0.459) [k = 1.14]	H→L (0.954)
2	2.77 <sup>a</sup>	2.88 (0.319)	2.72 (0.323) [ $k = 1.47$ ]	H→L (0.875)
3	2.32	2.54 (0.522)	$2.28 (0.469) \\ [k = 1.80]$	H→L (0.983)
4	3.21	3.26 (0.496)	3.20 (0.490) [ $k = 1.14$ ]	H→L (0.919)
5	3.35	3.38 (0.409)	3.32 (0.406) [ $k = 1.14$ ]	H-1→L (0.881)
6	3.47	3.47 (0.114) 3.53 (0.092) 3.59 (0.546) {3.56 <sup>b</sup> }	3.41 (0.113) 3.47 (0.088) 3.54 (0.577) (3.51 <sup>b</sup> } [k=1.14]	H-2 $\rightarrow$ L (0.769) H-1 $\rightarrow$ L (0.889) H $\rightarrow$ L (0.831)
7	2.95	3.06 (0.641)	2.83 (0.573) [k = 1.47] 2.98 (0.616) [k = 1.14]	H→L (0.911)

a Shoulder.

calculations with 6-31G\* level [15] support the nature of the bonds (Table 2).

The character of the naphthalene HOMO is maintained in the naphthalene unit for the HOMO of 1 from the LCAO coefficients of the HOMO using HMO calculations (Figs. 3 and 4). Similarly, the character of the naphthalene LUMO is maintained in the naphthalene unit for the LUMO of 1 (Figs. 3 and 4). The longest absorption band (the p-band) is considered to be  $\pi \to \pi^*$  transition of HOMO $\to$ LUMO by PPP MO calculations with the M·M- $\gamma$ . Therefore, the SP of 1 is the naphthalene unit as shown in Fig. 1. The excitation energy of the *p*-band of **1** calculated by PPP MO calculations using the new- $\gamma$  (k = 1.14: See Table 1) reproduced the observed value better than that by using the N·M-γ (Table 3). The calculated bond lengths also reproduced the observed ones, rather than those calculated by the ab initio method with 6-31G\* level (Table 2).

# 3.2. Benz[a]aceanthrylene (2), Dibenzo[a,d]aceanthrylene (3) and Benzo[k]fluoranthene (4)

From the LCAO coefficients of HOMO using HMO calculations, the character of the anthracene HOMO and LUMO are maintained in the anthracene unit for the HOMO and the LUMO of 2 (Figs. 3 and 4). Therefore, the SP of 2 is the anthracene unit (Fig. 1).

Similarly, the SP of 3 is determined to be the naphthacene unit (Figs. 1, 3 and 4). The excitation energies of the *p*-band of 2 and 3 calculated by PPP MO calculations using the new- $\gamma$  (k = 1.47 and 1.80: see Table 1) reproduced the observed values in comparison with that by using the N·M- $\gamma$  (Table 3).

For the HOMO of 4, the character of the naphthalene HOMO is maintained in both A and B naphthalene units (Fig. 3). The character of the naphthalene LUMO is only maintained in the A

b Weighted mean.

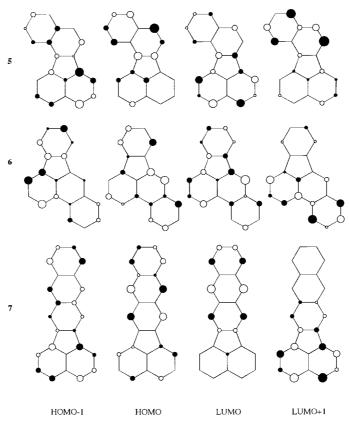


Fig. 5. The LCAO coefficients of HOMO-1, HOMO, LUMO and LUMO+1 of compounds 5, 6 and 7.

naphthalene unit for the LUMO of **4** (Fig. 3). Therefore, the SP of **4** is determined to be the **A** naphthalene unit (Fig. 1). The excitation energy of the *p*-band of **4** calculated by PPP MO calculations using the new-γ (k = 1.14: see Table 1) reproduced better the observed value in comparison with that using the N·M-γ (Table 3).

## 3.3. Benzo[i]fluoranthene (5)

The first absorption band (p-band) of **5** is considered to be a  $\pi \to \pi^*$  transition of HOMO-1 $\to$  LUMO by PPP MO calculations using the N·M- $\gamma$ . For the HOMO-1 of **5**, the character of the naphthalene HOMO is maintained in the **A** naphthalene unit (Fig. 5). The character of the naphthalene LUMO is maintained in the **A** naphthalene unit for the LUMO of **5** (Fig. 5). Therefore, the sp of **5** is determined to be the **A** naphthalene unit (Fig. 1). The excitation energies of the p-band of **5** calculated

by PPP MO calculations using the new- $\gamma$  (k = 1.14: see Table 1) reproduced well the observed value, as well as that using the N·M- $\gamma$  (Table 3).

# 3.4. Benzo[a]phenanthrylene (6)

The SP of phenanthrene is a naphthalene unit which is the longest acene-like portion in the molecular framework, as described in our previous papers [5,6]. However, the character of the HOMO or the LUMO of naphthalene cannot be seen in the HOMO-1, the HOMO, the LUMO and the LUMO+1 of 6 (Fig. 5).

From the PPP MO calculations using the N·M- $\gamma$ , the first absorption band of **6** is considered to be a  $\pi \to \pi^*$  transition of HOMO-2 $\to$ LUMO, the second absorption band is considered to be a  $\pi \to \pi^*$  transition of HOMO-1 $\to$ LUMO, and the third absorption band is considered to be a  $\pi \to \pi^*$  transition of HOMO $\to$ LUMO. The excitation

energies of the first, the second and the third absorption band are very close (Table 1). Thus, the observed excitation energy of the *p*-band may be the combination of the above three absorption bands.

We assumed that the SP of  $\bf 6$  is the naphthalene unit in the phenanthrene unit (Fig. 1) as is the case of phenanthrene, and calculated the excitation energies of  $\bf 6$  using the new- $\gamma$  (k=1.14: see Table 1). The weighted mean value of the calculated excitation energies of the first, the second and the third absorption bands reproduced the observed excitation energy of the p-band, in comparison with the calculated value using the N·M- $\gamma$  (Table 3).

## 3.5. Naphtho[2,3-k]phenanthrylene (7)

The longest acene-like portion in the molecular framework of 7 is the anthracene unit. For the HOMO and the LUMO of 7, the character of the anthracene HOMO and LUMO are maintained in the anthracene unit (Fig. 5). So we considered that the SP of 7 is the anthracene unit (Fig. 1). The excitation energy of the *p*-band was calculated by the PPP MO method using new- $\gamma$  (k=1.47: see Table 1). However, the calculated energy value was lower than the observed one (Table 3).

The bond length of the **hh** bond of 7 (1.458 Å) calculated by the ab initio method with 6-31G\* level, whose reliability is proved by the calculation of the bond lengths of 1, is longer than the bond length of the same position of anthracene (observed value:1.418 Å [16], calculated value by ab initio method with 6-31G\* level: 1.433 Å). The **hh** bond possesses the nature of single bond, though it is essentially contained in the  $\pi$ -conjugated system (Table 2). This character of 7 is different from that of 1 (See Table 2). Thus, the nature of anthracene seems to be weakened in the anthracene unit of 7. Therefore, we concluded the residual naphthalene unit in the anthracene unit to be SP (Fig. 1). The excitation energy of the p-band of 7 was calculated using the new- $\gamma$  (k = 1.14: see Table 1), and the result reproduced well the observed value (Table 3).

The bond lengths calculated by the PPP MO method using the new- $\gamma$  are closer to the those calculated by the ab initio method with 6-31G\*

level. However, its reliability could not be ascertained because of the absence of experimental values, to the best of our knowledge.

### 4. Conclusion

The SP was decided by the character of HOMO-1, HOMO, LUMO and LUMO+1, and was calculated by the HMO method for non-alternate PAHS 1–6 as alternate PAHs, and was decided referring the structural analysis using the ab initio calculation with 6-31G\* level for 7. The calculated excitation energies of the p-band using the PPP MO method with the new- $\gamma$  containing the SCS parameter k evaluated based on the SP reproduced the observed ones well, in comparison with data using the conventional N·M- $\gamma$ .

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